# Introduction to Machine Learning

Decision Trees

Varun Chandola

April 14, 2020

# Outline

# Contents

1 Explainable Machine Learning

# 1 Explainable Machine Learning

# Why Decision Trees?

• Linear models are easy to interpret/explain but have limited power

1

• Non-linear models can be more accurate but are "black-boxes"

## Why do we care about interpretability and explainability?

- Builds trust, transparency, and accountability into the model
- Needed for fairness and ethical considerations of ML





## **Decision Trees**

- Inherently "non-linear" model
- No linear boundary
- Divide the region  $(\mathcal{X})$  into non-intersecting sub-regions

$$\mathcal{X} = \bigcup_{i=0}^{n} R_i$$
s.t.  $R_i \cap R_j = \emptyset$ , for  $i \neq j$ 

#### How to select regions

- Computationally intractable
- Decision trees approximate solution via a greedy, top-down, recursive partitioning scheme.
- Start with  ${\mathcal X}$  and split it into two child regions by thresholding on a single feature

- Continue splitting nodes using a feature and a threshold
- Formally, given a parent region  $R_p$ , a feature index j, and a threshold  $t \in \mathbb{R}$ , we obtain two child regions as:

$$R_{p1} = \{ \mathbf{x} | x_j < t, \mathbf{x} \in R_p \}$$
  

$$R_{p2} = \{ \mathbf{x} | x_j \ge t, \mathbf{x} \in R_p \}$$

How to choose the splits?

- Need a loss function L() as a set function on a region R
- For a given parent  $R_p$ , we can calculate the decrease in loss as:

$$\delta = L(R_p) - \frac{|R_1|L(R_1) + |R_2|L(R_2)|}{|R_1| + |R_2|}$$

### **Cross-entropy Loss**

$$L_{cross}(R) = -\sum_{c} \hat{p}_c \log_2 \hat{p}_c$$

•  $\hat{p}_c$  is the probability of observing an example of class c in the given node

$$\hat{p}_c = \frac{|\mathbf{x} : class(\mathbf{x}) = c, \mathbf{x} \in R|}{|R|}$$

• If  $\hat{p}_c = 0$  then  $\hat{p} \log_2 \hat{p} \equiv 0$ 

#### Alternatives Cross-entropy Loss

Gini Index/Loss

$$L_{gini}(R) = 1 - \sum_{c} \hat{p}_{c}^{2}$$

### Other Considerations

- Categorical features
- Regularization (pruning)
- Computational complexity O(N \* D \* d)
  - $-\ N$  number of training examples
  - $-\ D$  number of features
  - $-\ d$  depth of the tree

## Variants of Decision Trees

- Regression Trees Use a different loss function
- Random Forests An ensemble of decision trees

# References